

Task 1 P1

Tyronne Helsdown

$$(i) \quad \begin{array}{l} M1 \quad 40 = 0.25M + 0.5E \\ M2 \quad 40 = 0.40M + 0.2E \end{array} \quad \begin{array}{l} \checkmark \\ \checkmark \end{array} \quad \begin{array}{l} M = \text{mechanical} \\ \text{Product} \end{array}$$

$$\Rightarrow \begin{array}{l} M1 \quad 80 = 0.5M + E \\ M2 \quad 200 = 2M + E \end{array} \quad \begin{array}{l} E = \text{Electronic} \\ \text{product} \end{array}$$

$$\Rightarrow 120 = 1.5M + 0$$

$$\Rightarrow M = \frac{120}{1.5} = \boxed{80} \quad \text{Mechanical components}$$

$$40 = 0.25(80) + 0.5E$$

$$\Rightarrow 40 = 20 + 0.5E$$

$$\Rightarrow 40 - 20 = 0.5E$$

$$\Rightarrow 20 = 0.5E$$

$$\Rightarrow E = \frac{20}{0.5} = \boxed{40} \quad \text{Electrical components}$$

$$40 = 0.25(80) + 0.5(40)$$

$$\Rightarrow 0.25(80) + 0.5(40) - 40 = 0$$

$$\Rightarrow 20 + 20 - 40 = 0$$

Task 1

$$M1 = 40 = 0.25M + 0.5E$$

$$\Rightarrow 40 - 0.25M = 0.5E$$

$$\Rightarrow E = \frac{0.25}{0.5}M - \frac{40}{0.5}$$

$$\Rightarrow E = 0.5M - 80$$

Electrical intercept

$$M1 \Rightarrow 40 - 0.5E = 0.25M$$

$$\Rightarrow M = \frac{0.5}{0.25}E - \frac{40}{0.25} \Rightarrow M = 2E - 160$$

Mechanical intercept

$$M2 = 40 = 0.4M + 0.2E$$

$$\Rightarrow 40 - 0.4M = 0.2E$$

$$\Rightarrow E = \frac{0.4}{0.2}M - \frac{40}{0.2}$$

$$\Rightarrow E = 2M - 200$$

Electrical intercept

$$M2 \Rightarrow 40 - 0.2E = 0.4M$$

$$\Rightarrow M = \frac{0.2}{0.4}E - \frac{40}{0.4}$$

$$\Rightarrow M = 0.5E - 100$$

Mechanical intercept

Task 1P1(i)

Table 1 $0.25x + 0.50y = 40$ (Machine 1)

$$0.25x = -0.50y + 40$$

$$x = \frac{-0.5}{0.25}y + \frac{40}{0.25}$$

$$x = -2(y) + 160$$

y(E)	0	10	20	30	40	50	60	70	80
x(M)	160	140	120	100	80	60	40	20	0

Table 2 $0.4x + 0.20y = 40$ (Machine 2)

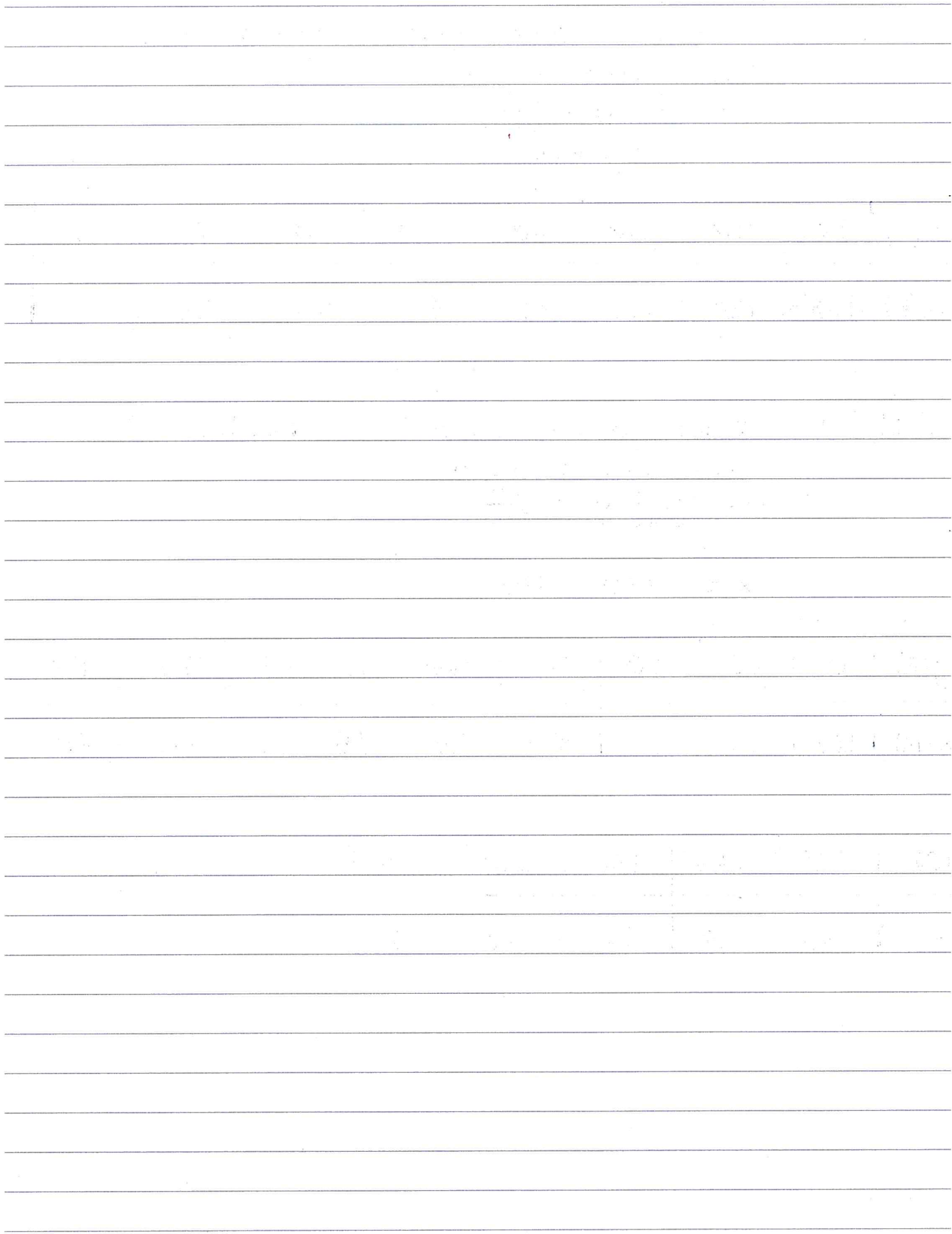
$$0.4x = -0.20y + 40$$

$$x = \frac{-0.20}{0.40}y + \frac{40}{0.40}$$

$$x = -0.5(y) + 100$$

y(E)	0	10	20	30	40	50	60	70	80
x(M)	100	95	90	85	80	75	70	65	60

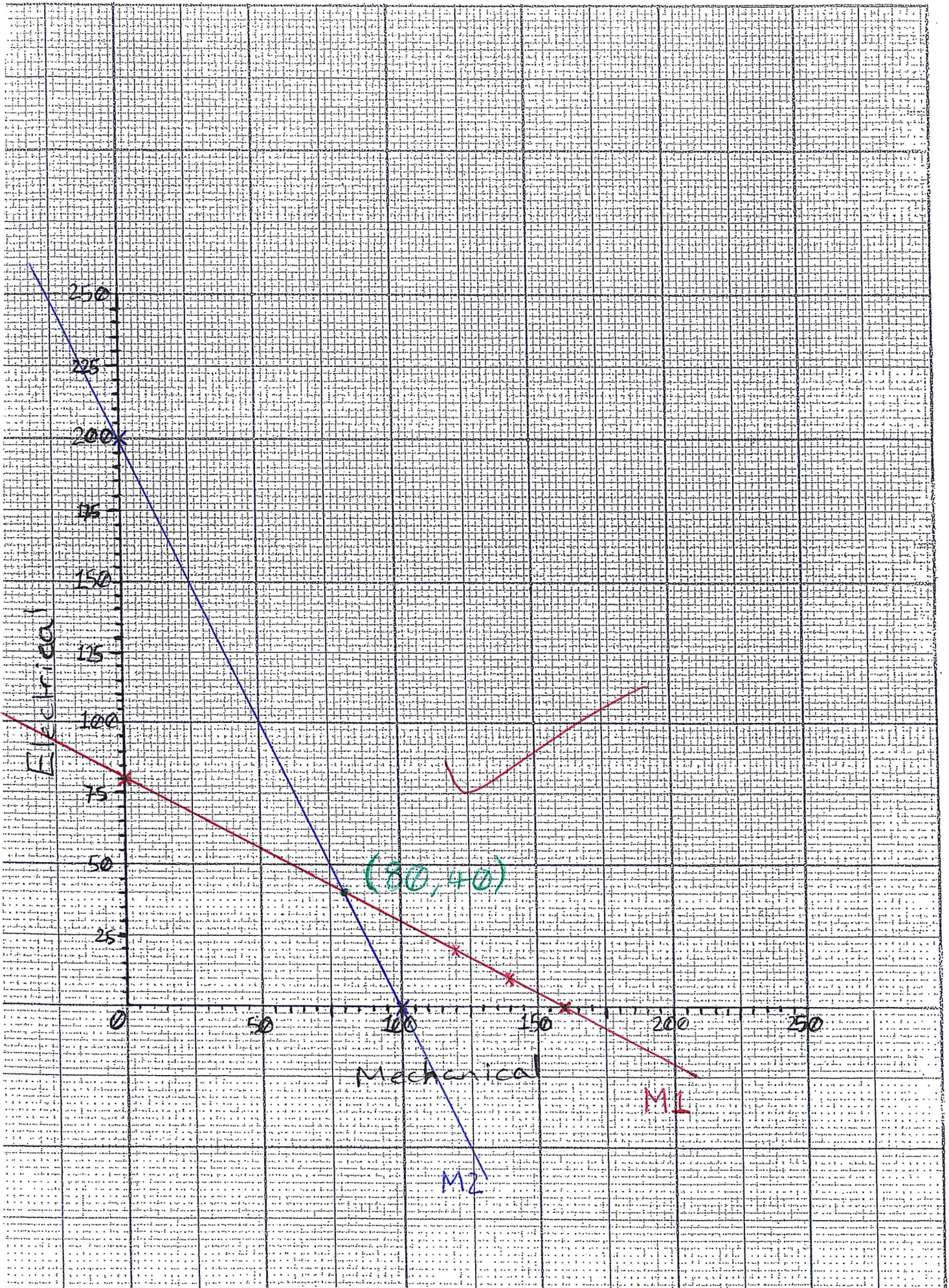
100	120	140	160	180	200
50	40	30	20	10	0



(iii)

Task 1 P1

Tyronne H



Task 1 M1

Tyrone H.

Voltage V volts	2.88	2.05	1.60	1.22	0.96
$\log V$	0.459	0.312	0.204	0.086	-0.018
Admittance Y Siemens	0.52	0.73	0.94	1.23	1.57
$\log Y$	-0.284	-0.137	-0.027	0.090	0.196

$$V = KY^n \quad (V, Y) = (2.88, 0.52), (1.22, 1.23)$$

$$2.88 = K(0.52)^n \quad \text{equation 1}$$

$$1.22 = K(1.23)^n \quad \text{equation 2}$$

$$\frac{2.88}{1.22} = \frac{K(0.52)^n}{K(1.23)^n} \rightarrow 2.361 = \left(\frac{0.52}{1.23}\right)^n$$

$$2.361 = 0.423^n \rightarrow \log 2.361 = \log 0.423^n$$

$$\rightarrow 0.373 = n(-0.374) \rightarrow n = -0.997 \text{ or } -1$$

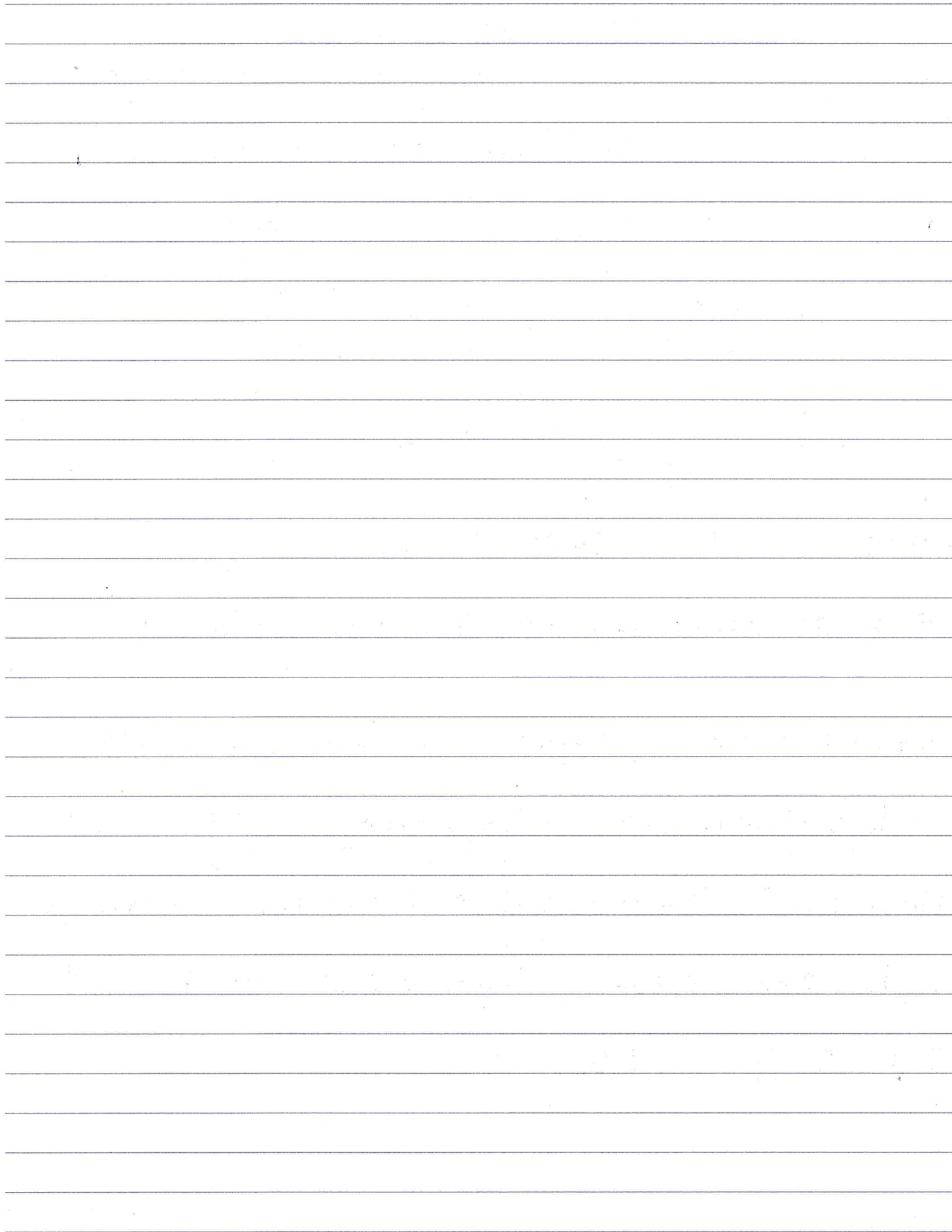
$$V = KY^n \rightarrow \log(V) = \log(KY^n) \rightarrow \log V = \log K + \log Y^n$$

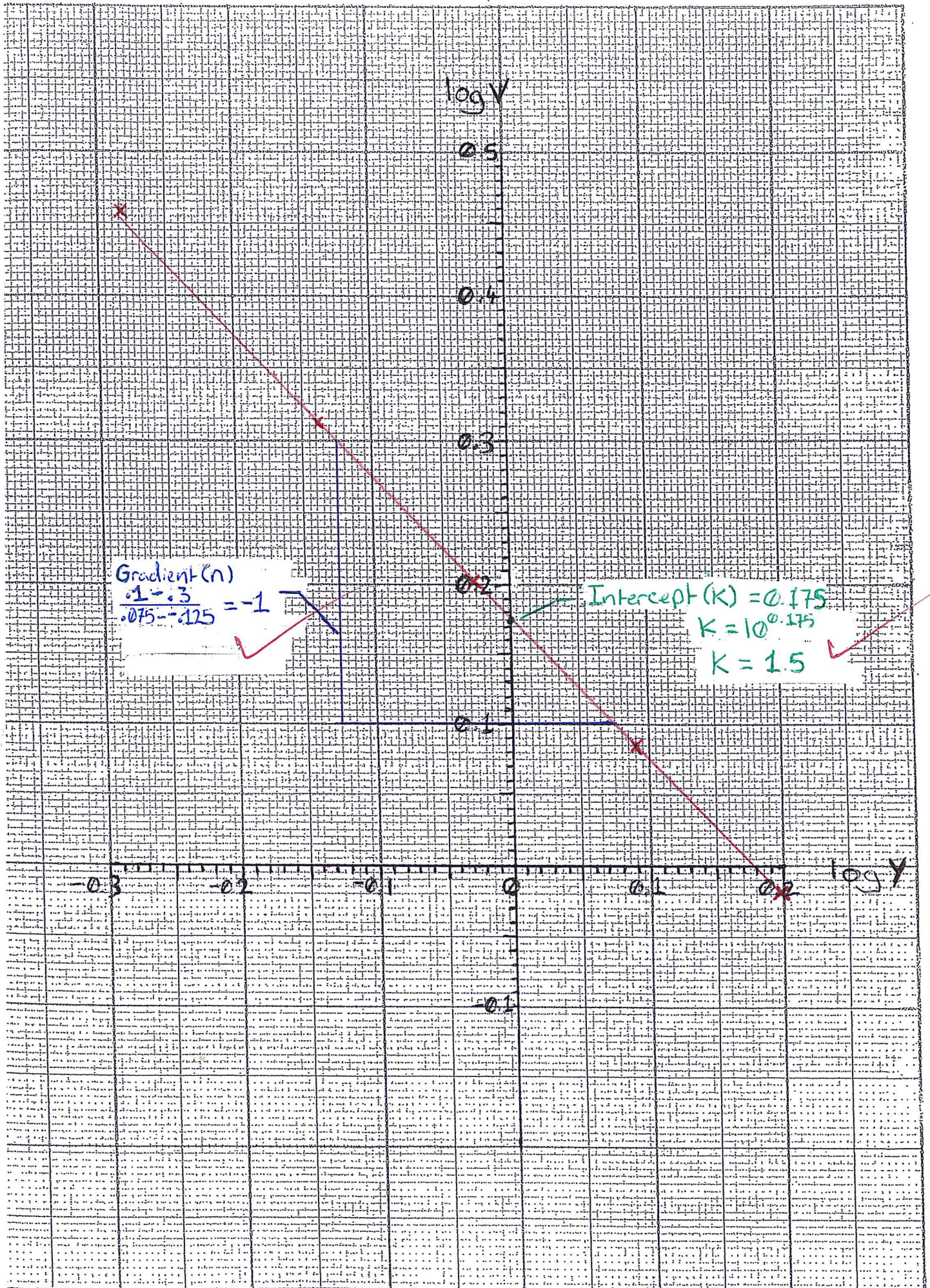
$$\rightarrow \log V = \log K + n \log Y \rightarrow \log V = n \log Y + \log K \quad \text{equation 3}$$

$$(\log V, \log Y) = (0.459, -0.284) \rightarrow 0.459 = -1(-0.284) + \log K \rightarrow$$

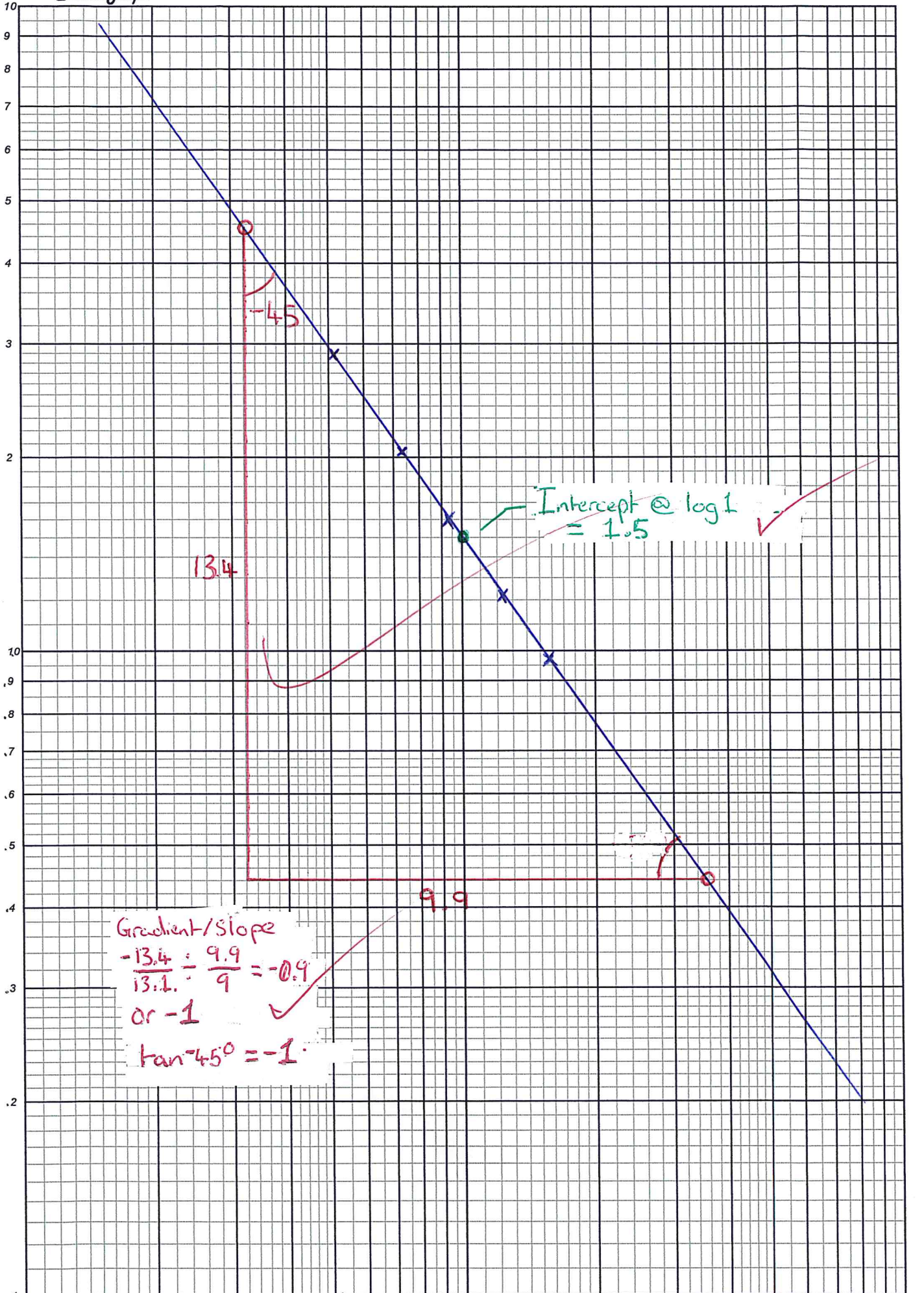
$$\log K = 0.459 - 0.284 \Rightarrow \log K = 0.175 \rightarrow K = 10^{0.175}$$

$$\rightarrow K = 1.496 \text{ or } 1.5$$





Custom Graph™



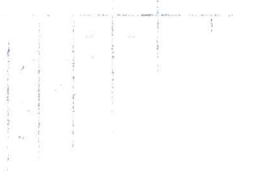
x

x

x

x

x



Task 1 M1 (c)

a) By converting the table to its logarithmic values, I was then able to construct a graph using linear graph paper. Considering the equation was in the form of $\log V = n \log Y + \log k$, the dependent variable was $\log V$ which I placed onto the y axis with $\log Y$ (the independent variable) on the x axis.

After plotting the points and marking the line on the paper I was able to confirm that the intercept was 0.175 by using antilog I arrived at my value for k of 1.5 which was obtained from the analytical method, I then found the gradient by choosing two points on the plot and calculated with $\frac{\Delta y}{\Delta x}$ in this case

$$\frac{.1 - .3}{.075 - -.125} = -1$$

, this was also in line with the results obtained analytically and confirmed that the law connecting the quantities is of the form $V = KY^n$

b) By using the values provided initially for the values of V and I was able to plot straight to a 2x2 cycle log-log graph, by using a scale of 0.0-1.0 for cycle 1 and 1-10 during the second, I could plot all of the points.

After plotting the points and determining the straight line I found 1 on the x axis, since $\log(1)$ is equal to zero this would be the y-intercept; therefore in accordance to the graph when $x = 1$, $y = 1.5$ this is what I was expecting to see and it was confirmed graphically. The gradient was found by measuring from two points separated on the line and creating a right angled triangle; by measuring the lengths I calculated the gradient, I had to divide the vertical length by the length of the vertical cycle and the horizontal length by the length of the horizontal cycle, because the cycle lengths were different.

$$\text{Hence } \frac{-13.4}{13.1} \div \frac{9.9}{9} = -0.9 = -1$$

as a check the slope angle measured -45° approximately with a protractor and the tangent of this is -1 , thus confirming the gradient.

with these results I confirmed the accuracy of the two graphs in relation to the law connecting the quantities

P2 (Task 2)

a) Given: Nth term = 80 $a = 30$ $d = 2$

$$\Sigma = \frac{n}{2}(2a + (n-1)d) \quad \Sigma = \frac{80}{2}(2 \cdot 30 + (80-1) \cdot 2) \Rightarrow \Sigma = \boxed{8720}$$

b) Given: $a = 100$ $8N = 1000$

$$a_n = a + (n-1)d \Rightarrow 1000 = 100 + (8-1)d \Rightarrow 900 = 7d$$

$$d = \frac{900}{7} = 128.57$$

$$1 = 100 \quad 2 = 100 + 1 \cdot 128.57 = 228.57 \rightarrow \boxed{229}$$

$$3 = 100 + 2 \cdot 128.57 = 357.14 = \boxed{357}$$

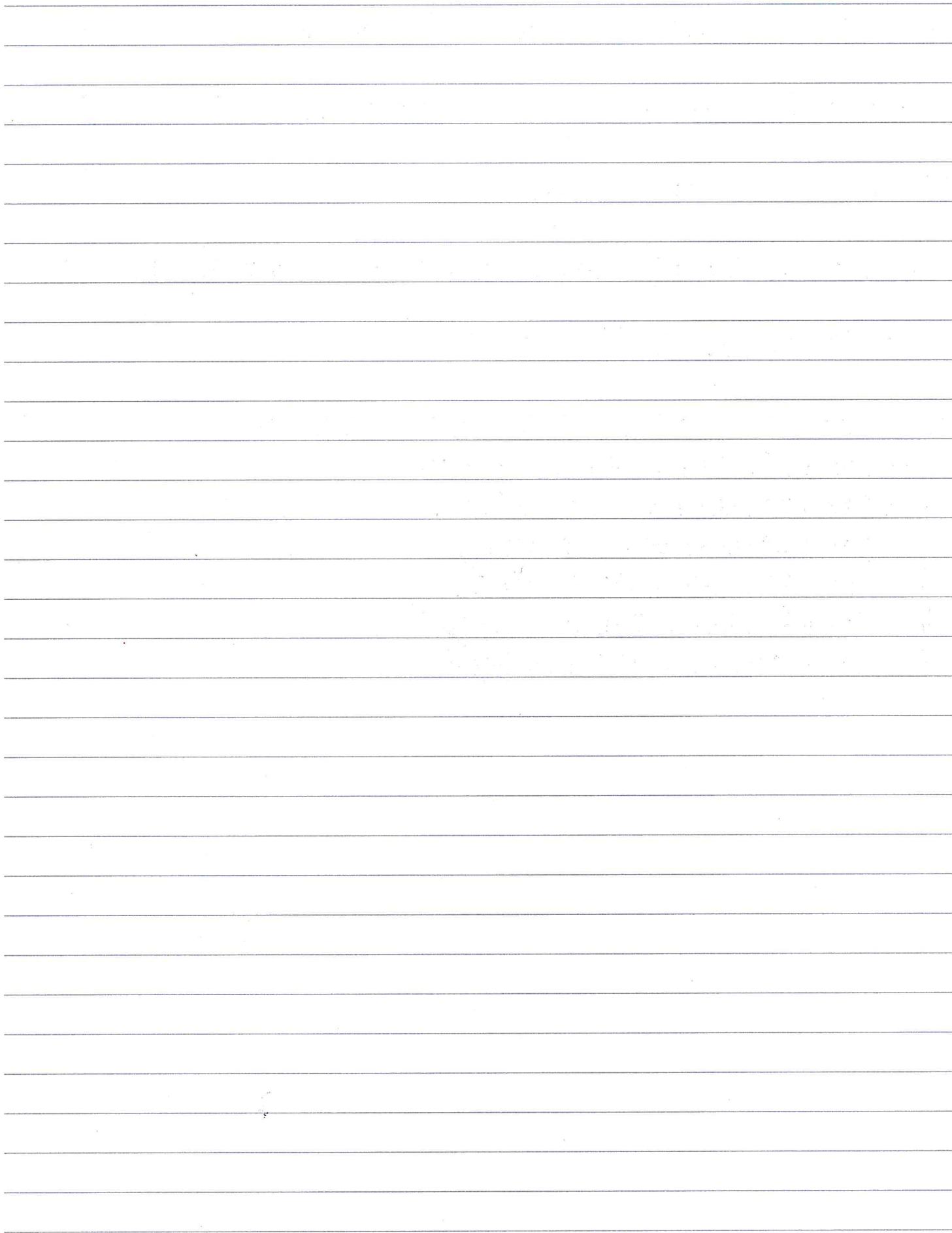
$$4 = 100 + 3 \cdot 128.57 = 485.71 = \boxed{486}$$

$$5 = 100 + 4 \cdot 128.57 = 614.28 = \boxed{614}$$

$$6 = 100 + 5 \cdot 128.57 = 742.85 = \boxed{743}$$

$$7 = 100 + 6 \cdot 128.57 = 871.42 = \boxed{871}$$

$$8 = 100 + 7 \cdot 128.57 = 999.99 = \boxed{1000}$$



Task 3 P3

a) Given: 8th term = 1000 $a = 100$ Find: $r = ?$

$$n^{\text{th}} = ar^{(n-1)} \rightarrow 1000 = 100r^{(8-1)} \rightarrow r^7 = \frac{1000}{100}$$

$$r = \sqrt[7]{10} \rightarrow r = 1.3895$$

$$1^{\text{st}} \text{ term} = a = \boxed{100}$$

$$2^{\text{nd}} \text{ term} = 100(1.3895)^{2-1} = 138.95 = \boxed{139 \text{ rev/min}}$$

$$3^{\text{rd}} \text{ term} = 100(1.3895)^{3-1} = 193.07 = \boxed{193 \text{ rev/min}}$$

$$4^{\text{th}} \text{ term} = 100(1.3895)^{4-1} = 268.27 = \boxed{268 \text{ rev/min}}$$

$$5^{\text{th}} \text{ term} = 100(1.3895)^{5-1} = 372.76 = \boxed{373 \text{ rev/min}}$$

$$6^{\text{th}} \text{ term} = 100(1.3895)^{6-1} = 517.96 = \boxed{518 \text{ rev/min}}$$

$$7^{\text{th}} \text{ term} = 100(1.3895)^{7-1} = 719.70 = \boxed{720 \text{ rev/min}}$$

$$8^{\text{th}} \text{ term} = 100(1.3895)^{8-1} = 1000.02 = \boxed{1000 \text{ rev/min}}$$

b) Given: Value = £3000 $r = 15\%$ annual decrease after each year, therefore $a - 15\% = 85\% a \rightarrow r = 0.85$ $a = £2550$

Find: Value for 4th year & nth year value < £550

$$4^{\text{th}} \text{ year} = 2550 (0.85)^{4-1} = \boxed{£1566}$$

$$550 = 2550 (0.85)^{n-1} \Rightarrow 0.85^{n-1} = \frac{550}{2550} \Rightarrow 0.85^{n-1} = 0.216$$

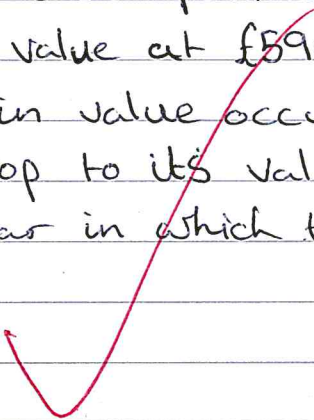
$$\Rightarrow \log(0.85)^{n-1} = \log(0.216) \Rightarrow (n-1) \log(0.85) = \log(0.216)$$

$$n-1 = \frac{\log(0.216)}{\log(0.85)} \Rightarrow n-1 = 9.45 \Rightarrow n = 10.45$$

$$10^{\text{th}} \text{ year} = 2550 (0.85)^{10-1} = £591$$

$$11^{\text{th}} \text{ year} = 2550 (0.85)^{11-1} = \boxed{£502}$$

Although the value of the lathe would technically drop below the £550 pound threshold part way through the 10th year, it started its value at £597, it is only when the next 15% reduction in value occurs; in the 11th year that it would drop to its value < £550 of £502, it's therefore the 11th year in which the lathe would be sold



Task 4 P4 Given $Z_1 = 1+j2$, $Z_2 = 4-j3$, $Z_3 = -2+j3$, $Z_4 = -5-j$

A)

$$1+j2 \Rightarrow z = r = \sqrt{(1)^2 + (2)^2} = 2.236 \quad \text{I quadrant}$$

$$\Rightarrow \arg z = \tan^{-1}\left(\frac{2}{1}\right) = 63.43^\circ \Rightarrow 1+j2 = 2.236 \angle 63.43^\circ$$

$$4-j3 \Rightarrow z = r = \sqrt{(4)^2 + (-3)^2} = 5 \quad \text{IV quadrant}$$

$$\Rightarrow \arg z = \tan^{-1}\left(\frac{-3}{4}\right) = -36.87^\circ$$

$$\Rightarrow 4-j3 = 5 \angle -36.87^\circ$$

-2

$$-2+j3 \Rightarrow z = r = \sqrt{(-2)^2 + (3)^2} = 3.61 \quad \text{II quadrant}$$

$$\Rightarrow \arg z = \tan^{-1}\left(\frac{3}{-2}\right) = 180^\circ - 56.31^\circ = 123.69^\circ$$

$$\Rightarrow -2+j3 = 3.61 \angle 123.69^\circ$$

$$-5-j \Rightarrow z = r = \sqrt{(-5)^2 + (-1)^2} = 5.099 \quad \text{III quadrant}$$

$$\Rightarrow \arg z = \tan^{-1}\left(\frac{-1}{-5}\right) = 11.31^\circ - 180^\circ = -168.69^\circ$$

$$\Rightarrow -5-j = 5.099 \angle -168.69^\circ$$

$$a) Z_1 Z_3 + Z_4 \Rightarrow (2.236 \angle 63.43^\circ)(3.61 \angle 123.69^\circ) + (5.099 \angle -168.69^\circ)$$

$$Z_1 Z_3 \Rightarrow (2.236 \cdot 3.61) \angle (63.43 + 123.69) = 8.07 \angle 187.39^\circ$$

$$x = r \cos \theta \quad \text{and} \quad y = r \sin \theta$$

$$8.07 \angle 187.39^\circ \textcircled{1} + 5.099 \angle -168.69^\circ \textcircled{2} \quad \text{Can't add or subtract in polar}$$

$$\textcircled{1} 8.07 \angle 187.39^\circ \Rightarrow x = r \cos \theta \Rightarrow 8.07 \cos(187.39) = -8$$

$$\Rightarrow y = r \sin \theta \Rightarrow 8.07 \sin(187.39) = -1$$

$$\Rightarrow 8.07 \angle 187.39^\circ = -8-j$$

② $5.099 \angle -168.69^\circ$ is given $Z_4 = -5 - j$

$$-8 - j + -5 - j \Rightarrow (-8 + -5) - (-j - j) = -13 - j2$$

$$-13 - j2 \Rightarrow Z = r = \sqrt{(-13)^2 + (-2)^2} = 13.153$$

$$\Rightarrow Z = \theta = \tan^{-1}\left(\frac{-2}{-13}\right) = 8.75$$

$$180 + 8.75 = 188.75^\circ \quad \text{or} \quad -180 + 8.75 = -171.25^\circ$$

$$-13 - j2 \Rightarrow \boxed{13.153 \angle 188.75^\circ} \quad \text{or} \quad \boxed{13.153 \angle -171.25^\circ}$$

Task 4 P4

$$A) b) \quad \frac{Z_1 + Z_3}{Z_2 - Z_4} \Rightarrow \frac{(1+j2) + (-2+j3)}{(4-j3) - (-5-j)} \quad \textcircled{1}$$

$$\textcircled{2}$$

$$\textcircled{1} (1+j2) + (-2+j3) \Rightarrow (1-2) + j(2+3) = -1+j5 \quad \textcircled{3} \quad \checkmark$$

$$\textcircled{2} (4-j3) - (-5-j) \Rightarrow (4-(-5)) - j(-3-(-1)) = 9-j2 \quad \textcircled{4} \quad \checkmark$$

$$\textcircled{3} \frac{-1+j5}{9-j2}$$

$$\textcircled{3} -1+j5 \Rightarrow z = r = \sqrt{(-1)^2 + (5)^2} = 5.099$$

$$\Rightarrow \arg z = \theta = \tan^{-1}\left(\frac{5}{-1}\right) \Rightarrow 78.69^\circ \Rightarrow 180^\circ - 78.69^\circ = 101.31^\circ$$

$$\Rightarrow r \angle \theta \Rightarrow 5.099 \angle 101.31^\circ \quad \checkmark$$

$$\textcircled{4} 9-j2 \Rightarrow z = r = \sqrt{(9)^2 + (-2)^2} = 9.220$$

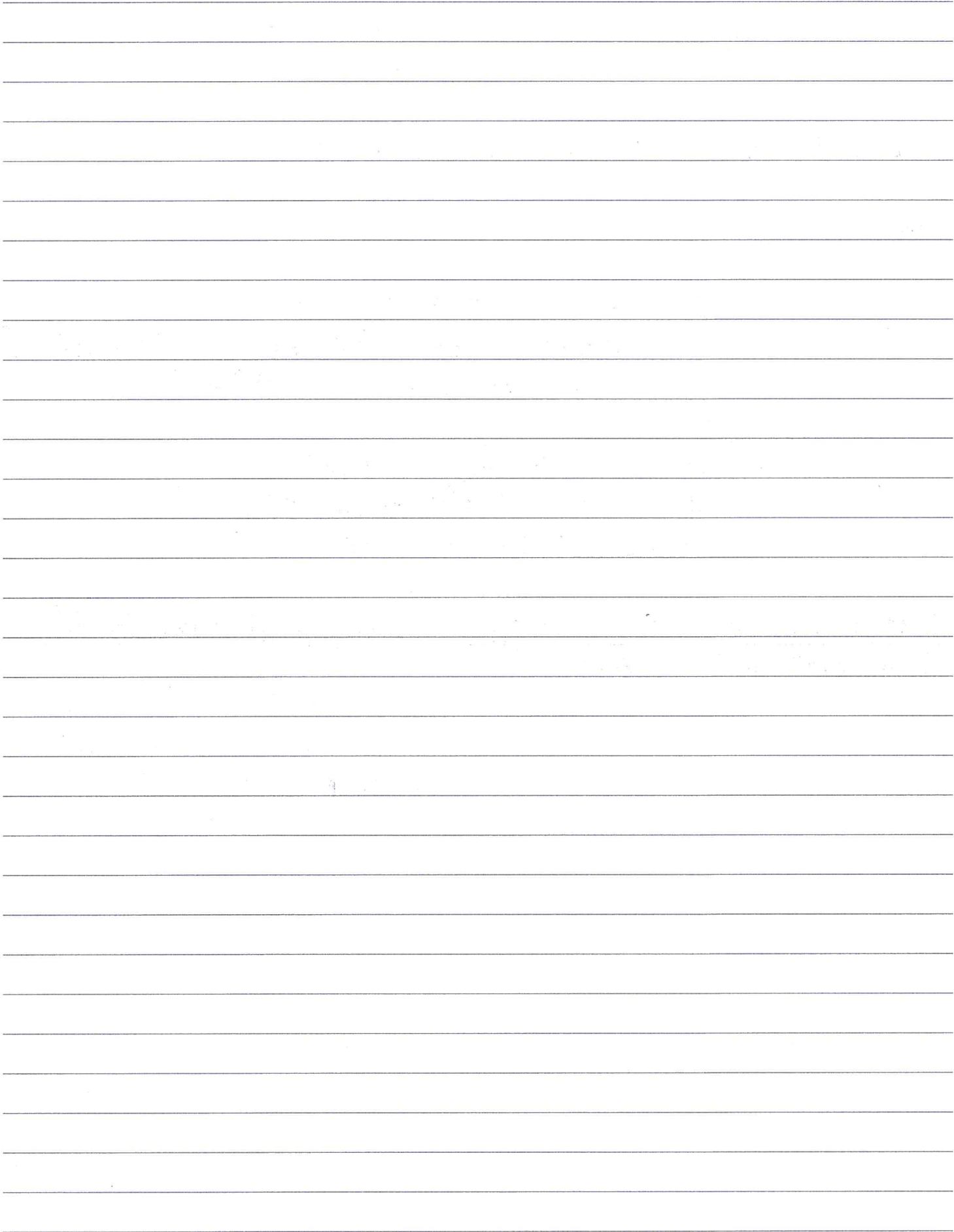
$$\Rightarrow \arg z = \theta = \tan^{-1}\left(\frac{-2}{9}\right) \Rightarrow -12.529^\circ$$

$$\Rightarrow r \angle \theta \Rightarrow 9.220 \angle -12.529^\circ \quad \checkmark$$

$$\frac{5.099 \angle 101.31^\circ}{9.220 \angle -12.529^\circ}$$

$$\frac{5.099}{9.220} \angle (101.31 - (-12.529)) = \boxed{0.553 \angle 113.839^\circ}$$

$$0.553 \cos(113.839) + j0.553 \sin(113.839) \\ -0.2225 + j0.506 \quad \checkmark$$



Task 4 P4 B)

$$a) 3 \angle 20^\circ \cdot 15 \angle 45^\circ \Rightarrow (3 \cdot 15) \angle (20 + 45) = 45 \angle 65^\circ$$

$$45 \angle 65^\circ \Rightarrow x = r \cos \theta \Rightarrow 45 \cos(65) = 19.018$$

$$y = r \sin \theta \Rightarrow 45 \sin(65) = 40.784$$

$$45 \angle 65^\circ \Rightarrow \boxed{19.018 + j40.784}$$

or

$$\textcircled{1} 3 \angle 20^\circ \cdot \textcircled{2} 15 \angle 45^\circ$$

$$\textcircled{1} 3 \angle 20^\circ \Rightarrow x = r \cos \theta \Rightarrow 3 \cos(20) = 2.819$$

$$y = r \sin \theta \Rightarrow 3 \sin(20) = 1.026$$

$$3 \angle 20^\circ \Rightarrow 2.819 + j1.026$$

$$\textcircled{2} 15 \angle 45^\circ \Rightarrow x = r \cos \theta \Rightarrow 15 \cos(45) = 10.607$$

$$y = r \sin \theta \Rightarrow 15 \sin(45) = 10.607$$

$$15 \angle 45^\circ \Rightarrow 10.607 + j10.607$$

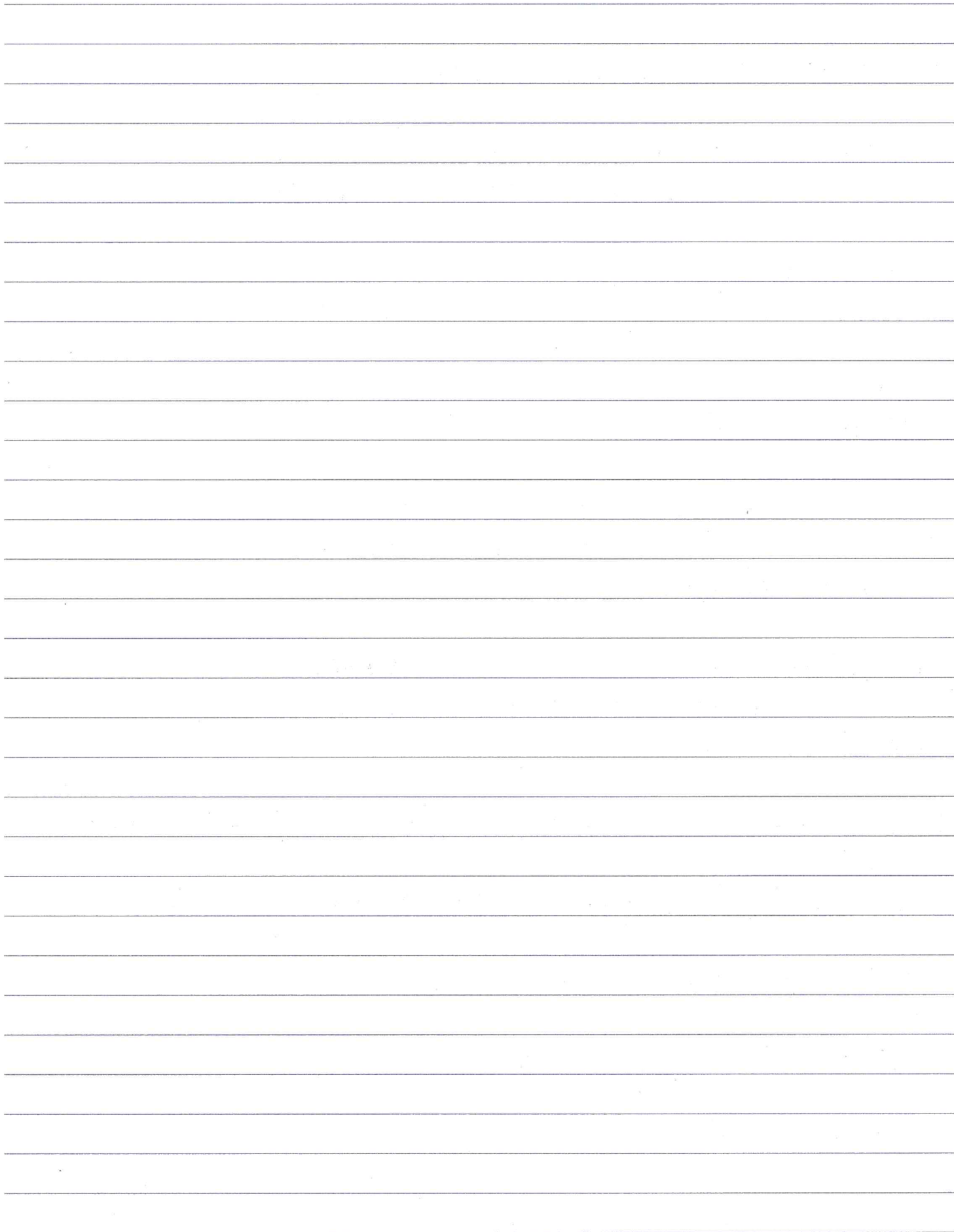
$$(2.819 + j1.026)(10.607 + j10.607) \Rightarrow 2.819(10.607 + j10.607) + j1.026(10.607 + j10.607)$$

$$\Rightarrow ((2.819 \cdot 10.607) + (j10.607 \cdot 2.819)) + ((j1.026 \cdot 10.607) + (j^2 \cdot (1.026 \cdot 10.607)))$$

$$\Rightarrow 29.901 + j29.901 + j10.883 + (-1) \cdot 10.883$$

$$\Rightarrow (29.901 - 10.883) + j(29.901 + 10.883)$$

$$= \boxed{19.018 + j40.784} \quad \text{or} \quad 45 \angle 65^\circ$$



Task 4 P4 B)

$$b) \textcircled{1} 2.4 \angle 65^\circ \times \textcircled{2} 4.4 \angle -21^\circ$$

$$\textcircled{1} 2.4 \angle 65^\circ \Rightarrow x = r \cos \theta \Rightarrow 2.4 \cos(65) = 1.014$$

$$y = r \sin \theta \Rightarrow 2.4 \sin(65) = 2.175$$

$$2.4 \angle 65^\circ = 1.014 + j2.175$$

$$\textcircled{2} 4.4 \angle -21^\circ \Rightarrow x = r \cos \theta \Rightarrow 4.4 \cos(-21) = 4.108$$

$$y = r \sin \theta \Rightarrow 4.4 \sin(-21) = -1.577$$

$$4.4 \angle -21^\circ = 4.108 - j1.577$$

$$(1.014 + j2.175)(4.108 - j1.577) \Rightarrow 1.014(4.108 - j1.577) + j2.175(4.108 - j1.577)$$

$$\Rightarrow ((1.014 \cdot 4.108) + (-j1.577 \cdot 1.014)) + ((j2.175 \cdot 4.108) + (j^2 \cdot (2.175 \cdot -1.577)))$$

$$\Rightarrow 4.166 - j1.599 + j8.935 + (-1) \cdot 3.430$$

$$\Rightarrow (4.166 + 3.43) + j(-1.599 + 8.935)$$

$$\Rightarrow \boxed{7.596 + j7.336}$$

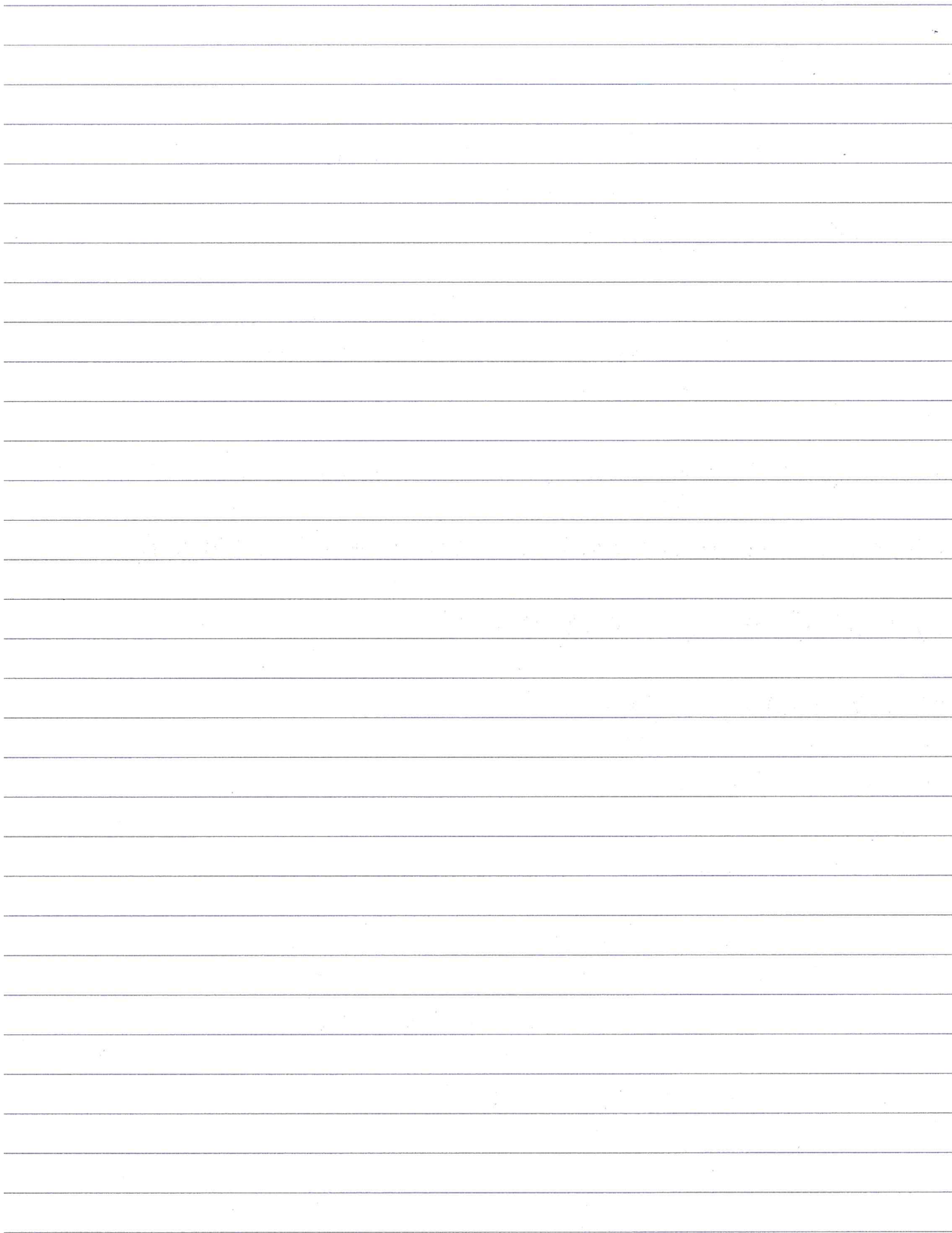
$$2.4 \angle 65^\circ \times 4.4 \angle -21^\circ$$

$$\Rightarrow (2.4 \cdot 4.4) \angle (65 + (-21)) = 10.56 \angle 44^\circ$$

$$x = r \cos \theta = 10.56 \cos(44) = 7.596$$

$$y = r \sin \theta = 10.56 \sin(44) = 7.336$$

$$10.56 \angle 44^\circ \Rightarrow \boxed{7.596 + j7.336}$$



Task 4 P4 B)

$$c) \textcircled{1} 5 \angle 30^\circ \times \textcircled{2} 4 \angle 80^\circ \div \textcircled{3} 10 \angle -40^\circ$$

$$\textcircled{1} 5 \angle 30^\circ \Rightarrow x = r \cos \theta \Rightarrow 5 \cos(30) = 4.33$$

$$y = r \sin \theta \Rightarrow 5 \sin(30) = 2.5$$

$$5 \angle 30^\circ \Rightarrow 4.33 + j2.5$$

$$\textcircled{2} 4 \angle 80^\circ \Rightarrow x = r \cos \theta \Rightarrow 4 \cos(80) = 0.695$$

$$y = r \sin \theta \Rightarrow 4 \sin(80) = 3.939$$

$$4 \angle 80^\circ \Rightarrow 0.695 + j3.939$$

$$\textcircled{3} 10 \angle -40^\circ \Rightarrow x = r \cos \theta \Rightarrow 10 \cos(-40) = 7.66$$

$$y = r \sin \theta \Rightarrow 10 \sin(-40) = -6.428$$

$$10 \angle -40^\circ \Rightarrow 7.66 - j6.428$$

$$\textcircled{4} (4.33 + j2.5)(0.695 + j3.939) / (7.66 - j6.428)$$

$$\textcircled{4} (4.33 + j2.5)(0.695 + j3.939) \Rightarrow 4.33(0.695 + j3.939) + j2.5(0.695 + j3.939)$$

$$\Rightarrow ((4.33 \cdot 0.695) + (j3.939 \cdot 4.33)) + ((j2.5 \cdot 0.695) + (j^2(2.5 \cdot 3.939)))$$

$$\Rightarrow 3.009 + j17.056 + j1.738 + ((-1) \cdot 9.848)$$

$$\Rightarrow (3.009 - 9.848) + j(17.056 + 1.738)$$

$$\Rightarrow -6.839 + j18.794$$

$$\frac{-6.839 + j18.794}{7.66 - j6.428} \Rightarrow \frac{-6.839 + j18.794}{7.66 - j6.428} \times \frac{7.66 + j6.428}{7.66 + j6.428}$$

$$\Rightarrow \frac{-6.839(7.66 + j6.428) + j18.794(7.66 + j6.428)}{(7.66 - j6.428)(7.66 + j6.428)}$$

$$\Rightarrow \frac{((-6.839 \cdot 7.66) + (j6.428 \cdot -6.839)) + ((j18.794 \cdot 7.66) + (j^2(18.794 \cdot 6.428))}{(7.66)^2 - (j6.428)^2}$$

$$\Rightarrow \frac{-52.387 - j43.961 + j143.962 + ((-1) \cdot 120.808)}{58.676 - j^2 41.319}$$

$$\Rightarrow \frac{(-52.387 - 120.808) + j(-43.961 + 143.962)}{58.676 - (-1) \cdot 41.319}$$

$$\Rightarrow \frac{-173.195 + j100.001}{99.995} \Rightarrow \frac{-173.195}{99.995} + j \frac{100.001}{99.995}$$

$$\Rightarrow \boxed{-1.732 + j}$$

$$5 \angle 30^\circ \times 4 \angle 80^\circ \div 10 \angle -40^\circ \Rightarrow (5 \angle 30^\circ)(4 \angle 80^\circ) \Rightarrow (5 \cdot 4) \angle (30 + 80)$$

$$\Rightarrow 20 \angle 110^\circ \Rightarrow (20 \angle 110^\circ) / 10 \angle -40^\circ \Rightarrow \left(\frac{20}{10}\right) \angle 110 - (-40)$$

$$= 2 \angle 150^\circ \quad x = r \cos \theta \Rightarrow 2 \cos(150) = -1.732$$

$$y = r \sin \theta \Rightarrow 2 \sin(150) = 1$$

$$2 \angle 150^\circ \Rightarrow \boxed{-1.732 + j}$$

Task 4 M2

a) Given :- $Z_1 = (3+j6)\Omega$, $Z_2 = (4-j3)\Omega$

$$Y = \frac{1}{Z_1} + \frac{1}{Z_2} \Rightarrow \frac{1}{3+j6} + \frac{1}{4-j3}$$

$$\textcircled{1} \frac{1}{3+j6} \Rightarrow \frac{1}{3+j6} \times \frac{3-j6}{3-j6} \Rightarrow \frac{3-j6}{(3)^2+(6)^2} = \frac{3}{45} - j\frac{6}{45} = 0.06 - j0.13$$

$$\textcircled{2} \frac{1}{4-j3} \Rightarrow \frac{1}{4-j3} \times \frac{4+j3}{4+j3} \Rightarrow \frac{4+j3}{(4)^2+(3)^2} = \frac{4}{25} + j\frac{3}{25} = 0.16 + j0.12$$

$$\frac{1}{3+j6} + \frac{1}{4-j3} \Rightarrow 0.06 - j0.13 + 0.16 + j0.12$$

$$\Rightarrow (0.06+0.16) + j(-0.13+0.12) = 0.22 - j0.01$$

$$Y = 0.22 - j0.01 \Rightarrow 0.22 \angle -2.603^\circ$$

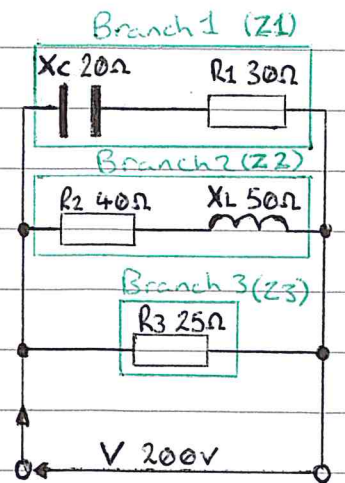
$$\begin{aligned} I &= \frac{V}{Z} = VY = (120 \angle 0^\circ)(0.22 \angle -2.603^\circ) \\ &= (120 \cdot 0.22) (\angle 0^\circ - 2.603^\circ) \\ &= 26.4 \angle -2.603^\circ \end{aligned}$$

The magnitude of current is equal to 26.4 A
it lags the voltage by 2.603°

Task 4 M2

- b) Given ① Branch 1; $X_C = 20\Omega$ $R_1 = 30\Omega$
 ② Branch 2; $R_2 = 40\Omega$ $X_L = 50\Omega$
 ③ Branch 3; $R_3 = 25\Omega$

$$Y = \frac{1}{Z_1} + \frac{1}{Z_2} + \frac{1}{Z_3}$$



$$\textcircled{1} Z_1 = R - jX_C \Rightarrow 30 - j20$$

$$\textcircled{2} Z_2 = R + jX_L \Rightarrow 40 + j50$$

$$\textcircled{3} Z_3 = 25\Omega$$

$$Y_1 = \frac{1}{Z_1} \Rightarrow \frac{1}{30 - j20} \Rightarrow \frac{1}{30 - j20} \times \frac{30 + j20}{30 + j20} \Rightarrow \frac{30 + j20}{(30)^2 + (20)^2}$$

$$\Rightarrow \frac{30}{1300} + j \frac{20}{1300} = 0.023 + j0.015 \text{ Siemens}$$

$$Y_2 = \frac{1}{Z_2} \Rightarrow \frac{1}{40 + j50} \Rightarrow \frac{1}{40 + j50} \times \frac{40 - j50}{40 - j50} \Rightarrow \frac{40 - j50}{(40)^2 + (50)^2}$$

$$\Rightarrow \frac{40}{4100} - j \frac{50}{4100} = 0.010 - j0.012 \text{ Siemens}$$

$$Y_3 = \frac{1}{Z_3} \Rightarrow \frac{1}{25} = 0.04 \text{ Siemens}$$

$$Y = \frac{1}{Z_1} + \frac{1}{Z_2} + \frac{1}{Z_3} \Rightarrow (0.023 + j0.015) + (0.01 - j0.012) + (0.04)$$

$$\Rightarrow (0.023 + 0.01 + 0.04) + j(0.015 - 0.012) = 0.073 + j0.003$$

$$\Rightarrow Z = r = \sqrt{(0.073)^2 + (0.003)^2} = 0.073$$

$$\arg Z = \tan^{-1}\left(\frac{0.003}{0.073}\right) = 2.353^\circ \Rightarrow 0.073 \angle 2.353^\circ$$

$$\begin{aligned} I &= \frac{V}{Z} = VY \Rightarrow (200 \angle 0^\circ) (0.073 \angle 2.353^\circ) \\ &\Rightarrow (200 \cdot 0.073) (\angle 0^\circ + 2.353^\circ) \\ &\Rightarrow 14.6 \angle 2.353^\circ \end{aligned}$$

$$\begin{aligned} 14.6 \angle 2.353^\circ &\Rightarrow x = r \cos \theta \Rightarrow 14.6 \cos(2.353) = 14.588 \\ &\Rightarrow y = r \sin \theta \Rightarrow 14.6 \sin(2.353) = 0.599 \end{aligned}$$

$$14.6 \angle 2.353^\circ = \boxed{14.588 + j0.599}$$

The magnitude of current is 14.588A and it leads the voltage by 2.353°